**CSC3060 AIDA – Assignment 1**

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# Introduction

## Report Structure

This report contains three sections of the assignment (Devereux, 2019).

Each section contains the following headings 1) Requirements. This part states the requirement and the expectations of the current section. 2) Assumption. If applicable, this part states any assumption we use when interpreting the requirement. The implementation is also based on the assumption. 3) Implementation. This part describes how the section is implemented in high level. 4) Result. This part states the result of the implementation and how to rerun the program.

# Section 1

## Requirements

The section 1 of the assignment (Devereux, 2019) requires 160 CSV files that represent images of four living things (cherry, pear, banana and flower) and four non-living things (envelope, golf club, pencil and wineglass). Each CSV file is 50 pixels by 50 pixels image which represents an instance of one thing, and there should be 20 instances for each thing.

The CSV file should be tab-delimited. Each value is either 0 or 1, representing if the corresponding pixel is black.

## Implementation

### Doodle Drawing

160 doodle images with 50 by 50 points were drawn on GIMP using my finger. They were then exported to PGM format with raw type.

### Doodle Examples

### Data Transformation

The PGM images were transformed into CSV files using Python. With the functions and , the data were loaded into Numpy arrays. They were then exported to CSV files with delimitations of tabs.

## Result

160 PGM files named as STUDENTNR\_LABEL\_INDEX. STUDENTNR is my student number which is 40216004. LABEL is the name of the thing/object. INDEX is the index of the instance. They are stored at the directory *section1\_images*.

The Python script stored at the directory *section1\_code* is used to generate the CSV files.

To run the Python script, make sure

* The Python package Pyyaml is installed
* The Python package Pillow is installed
* The current working directory is *section2\_code*

Then execute the command

The 160 corresponding CSV file will be generated which meet the Requirements.

# Section 2

## Requirements

Section 2 of the assignment (Devereux, 2019) requires to calculate twenty features for each instance, and store them into a CSV file.

The CSV file should be tab-delimited and contain 160 rows representing 160 instances. The rows should be sorted first by the label and secondly by the index. Each row contains the label and index of the instance, followed by the values of twenty features.

## Assumption

We assume any pixel out of the range of the image is white. For example, in a 50 by 50 image, the pixels and are white.

## Implementation

This section is implemented in Python.

#### configuration.yml

This file contains the configurations (e.g. names of objects, index range, names of features) of this section.

It makes the Python script more dynamic, and it is easier to control what the features and objects are processed. For example, if there is a need to drop features, change object labels or change the number of instances for each object, changing the configuration file is the only thing needed.

#### runme.py

This is the main Python script to be run to generate the CSV file containing feature values.

This is a controller of all objects. It reads a list of labels (i.e. object names) from the configuration file and calls the class Label for each label.

#### label.py

This is a controller of each object. The constructor of the class Label receives the label of the current object. It gets the range of the indices of instances from the configuration file, and call the class Instance for each instance.

#### instance.py

This is a controller of each instance. The constructor of the class Instance receives the label and index of the current instance.

It retrieves a list of feature’s names from the configuration file and calls the classes for each feature in the list. The classes of each feature will return the feature value. Then it writes the feature values to the output file.

#### features.py

This is a controller of each feature. The class of each feature receives the image data and the feature dictionary containing feature values of the current instance.

Each class of a specific feature extends the superclass Feature, which provides facilities and variables that helps compute and return the value of the current feature.

## Features

### Label

#### Name & Type

The name is . The type is string.

#### Implementation

It indicates the name of the thing.

### Index

#### Name & Type

The name is . The type is integer.

#### Implementation

It indicates the index of the instance of the thing.

### Feature 1

#### Name & Type

The name is . The type is integer.

#### Implementation

We iterates each pixel and check it is black. A counter is used to count the total number of black pixels.

### Feature 2

#### Name & Type

The name is . The type is integer.

#### Implementation

Two pixels on the top row and the bottom row among all black pixels are selected respectively. The value of the feature is the vertical distance between these two pixels.

### Feature 3

#### Name & Type

The name is . The type is integer.

#### Implementation

Two pixels on the most-left row and the most-right row among all black pixels were selected respectively. The value of the feature is the horizontal distance between these two pixels.

### Feature 4

#### Name & Type

The name is . The type is float.

#### Implementation

The distances between every two black pixels are calculated. Then they are compared, and the maximum value is selected as the value of this feature.

### Feature 5

#### Name & Type

The name is . The type is integer.

#### Implementation

The image data is iterated row by row. For each row, if five black pixels are found, this row is counted. The value of this feature is the number of counted rows.

### Feature 6

#### Name & Type

The name is . The type is integer.

#### Implementation

The image data is iterated column by column. For each column, if five black pixels are found, this column is counted. The value of this feature is the number of counted columns.

### Feature 7

#### Name & Type

The name is . The type is integer.

#### Implementation

For each black pixel in the image, if only one of its neighbours is black, the current black pixel is counted. The value of this feature is the number of counted black pixels.

### Feature 8

#### Name & Type

The name is . The type is integer.

#### Implementation

For each black pixel in the image, if only five of its neighbours are black, the current black pixel is counted. The value of this feature is the number of counted black pixels.

### Feature 9

#### Name & Type

The name is . The type is integer.

#### Implementation

For each 2-tile containing at least one pixel which is in the range of the image, if the two pixels of its most two left entries are black, and the remaining pixels are white, this 2-tile is counted. The value of this feature is the number of counted 2-tiles.

### Feature 10

#### Name & Type

The name is . The type is integer.

#### Implementation

For each 2-tile containing at least one pixel which is in the range of the image, if the two pixels of its most two right entries are black, and the remaining pixels are white, this 2-tile is counted. The value of this feature is the number of counted 2-tiles.

### Feature 11

#### Name & Type

The name is . The type is float.

#### Implementation

The value of this feature is .

### Feature 12

#### Name & Type

The name is . The type is integer.

#### Implementation

For each 2-tile containing at least one pixel which is in the range of the image, if the two pixels of its two top entries are black, and the remaining pixels are white, this 2-tile is counted. The value of this feature is the number of counted 2-tiles.

### Feature 13

#### Name & Type

The name is . The type is integer.

#### Implementation

For each 2-tile containing at least one pixel which is in the range of the image, if the two pixels of its two bottom entries are black, and the remaining pixels are white, this 2-tile is counted. The value of this feature is the number of counted 2-tiles.

### Feature 14

#### Name & Type

The name is . The type is float.

#### Implementation

The value of this feature is .

### Feature 15

#### Name & Type

This is a custom feature. The name is . The type is integer.

#### Feature Description

The value of this feature is the number of 3-tiles that the number of its black pixels is greater than the number of its white pixels. As a 3-tile has 9 pixels, it is equivalent to only counting the 3-tiles that has at least five black pixels. For example, Figure 1 is a 3-tile meeting this requirement (six black pixels > three white pixels), while Figure 2 is not.

|  |  |  |
| --- | --- | --- |
|  |  |  |
|  |  |  |
|  |  |  |

Figure Counted 3-tile

|  |  |  |
| --- | --- | --- |
|  |  |  |
|  |  |  |
|  |  |  |

Figure Not Counted 3-tile

#### Reason for Design

This measures how much the black pixels are concentrated together. This feature will have obvious values for the images of bananas and pencils. Both of them (Figure 3) have a considerable large area fulfilled with black pixels, while others do not. This will help us distinguish these two things from others. Also, then the size of the area in pencils is slightly larger than that in bananas on average, it also helps differentiate between these two things.

Figure Images of banana and pencil

#### Implementation

For each 3-tile containing at least one pixel which is in the range of the image, if five black pixels are found in the tile, this 3-tile is counted. The value of this feature is the number of counted 3-tiles.

### Feature 16

#### Name & Type

This is a custom feature. The name is . The type is integer.

#### Feature Description

The value of this feature is the number of unique 3-tiles in the image that meet either of the following requirement.

* Only these three pixels in the tile are black. Other pixels are white.
* Only these three pixels in the tile are black. Other pixels are white.

For example, Figure 4 is a 3-tile meeting the requirement.

|  |  |  |
| --- | --- | --- |
|  |  |  |
|  |  |  |
|  |  |  |

Figure Counted tile in Crossness

#### Reason of Design

This feature measures the crossness of things/objects. Especially, the images of bananas, envelope, golf clubs and pencils (Figure 5) contain many cross lines (neither vertical nor horizontal, but straight lines) that contribute to this feature. However, the deviation of this feature for golf clubs may be large, because some handles in the images of golf clubs are double-lines which do not meet the requirement of this feature.

Figure Things for Feature 16

#### Implementation

For each 3-tile containing at least one pixel which is in the range of the image, we find all black pixels in the tile. If the black pixels meet the requirement, this tile is counted. The final value is the number of counted 3-tiles.

### Feature 17

#### Name & Type

The name is . The type is integer.

#### Implementation

To calculate this feature, we find all black pixels in the image stored in list . In a LOOP, we first create a list , and move the first pixel of list to list . Then we keep searching for the neighbours of the pixels of list from list , until all neighbours of pixels of list are included in list . We continue the LOOP until the list is empty. The value of this feature is the number of list ’s.

The logic of the implementation is that each list is a connected region of black pixels. We move pixels from list to list to prevent the same pixel is searched more than once.

For example, for Figure 6, three list ’s of black pixels will be generated.

1. List of black pixels for the outer shape
2. List of black pixels for the first black bar in the middle
3. List of black pixels for the second black bar in the middle

Thus, the value of this feature for this image is 3.



Figure An Example for Feature 17

### Feature 18

#### Name & Type

The name is . The type is integer.

#### Implementation

We find all white pixels in the image, and use a similar technique in Feature 17 to get a list of list ’s. each list is a connected region of white pixels. A small difference for this feature is that we only consider two pixels are neighbours if they share the same edge.

After this, each list is a potential eye. A list is considered as an eye if it does not contain any pixel that is at the edge of the image. The value of this feature is the number of counted list ’s.

For example, for Figure 7, three list ’s of white pixels will be generated.

1. List of white pixels outside of the envelop shape
2. List of white pixels in the top region of the envelope
3. List of white pixels in the bottom region of the envelope



Figure An example of feature 18

The list 1 is not counted, because it contains at least one pixel which is at the edge of the image (e.g. pixel ), while both lists 2 and 3 do not. Lists 2 and 3 are counted, and the final value is 2.

### Feature 19

#### Name & Type

The name is . The type is float.

#### Implementation

We use the technique in Feature 18 to get a list of eyes (i.e. a list of counted list ’s). We count the number of white pixels in these eyes, marked as value . The value of this feature is .

### Feature 20

#### Name & Type

This is a custom feature. The name is . The type is integer.

#### Feature Description

The value of this feature is the maximum number of black pixels in the image that these black pixels are LINEAR. A group of pixels are LINEAR if all pixels are in the same vertical or horizontal line. (e.g. pixels are LINEAR because they are in the line ).

#### Reason for Design

The feature counts the max length of black pixels in the images. Some things have long straight lines (Figure 8), such as envelopes, flowers and wine glasses. Because their vertical or horizontal lines contribute to this feature, they have large values for this feature. Thus, it will be easy to distinguish them from other things by this feature.

Figure Examples for Feature 20

#### Implementation

First, all vertical and horizontal lines are found, and a list is generated where each element in the list is a line. We then count the black pixels in each line. The line with the greatest number of black pixels is the line we select. The value of this feature is the number of black pixels in the selected line.

## Result

All features are correctly implemented in Python.

To run the Python script, make sure

* The Python package Pyyaml is installed
* The current working directory is *section2\_code*

Then execute the command

A file called *40216004\_features.csv* will be generated and stored under the folder *section2\_features*.

The format of the CSV file meets the Requirements.

To examine the implementation of each feature, please see *features.py* under the directory *section2\_code/python\_modules.*

# Section 3

## Requirements

## Implementation

For each question, there is a corresponding folder under the directory *section3\_code* with the name of the index of the question. Under that folder, there is a runme.R file where is the start point of the R script. To rerun the R script for each question, make sure

* The current working directory is *section3\_code/questionX*, where X is the index of the question. (e.g. *section3\_code/question1*)
* All R libraries in the R script *section3\_code/utilities/libraries.R* are installed

Then execute the command

The figures/graphs will be generated at the directory *section3\_code/questionX/output*, where X is the index of the question.

## Subtask 1

### Requirement

Three features (nr\_pix, height and cols\_with\_5) are needed to be analysed, and we need to perform them on three groups (full set, non-living and living) of things. Hence, there are nine combinations.

### Implementation

For each combination, we have two figures. The first figure is the histogram of the distribution with a green line indicating the density of the distribution, and a red line showing the normal distribution of the sample mean and standard deviation. The second figure is a GG Plot which demonstrates the association between theoretical quantiles and actual quantiles.

### Reasoning

We use histogram and Q-Q line for the analysation. By using histogram with density line, we can identify the shapes of the distributions. We use Q-Q line to see the normality of the distributions.

### Result

#### nr\_pix

For the shape of the distribution of feature *nr\_pix* for full set, Figure 9 shows that the modality is unimodal, and the skewness is right skew. Figure 10 illustrates that the normality of the distribution is right skew.

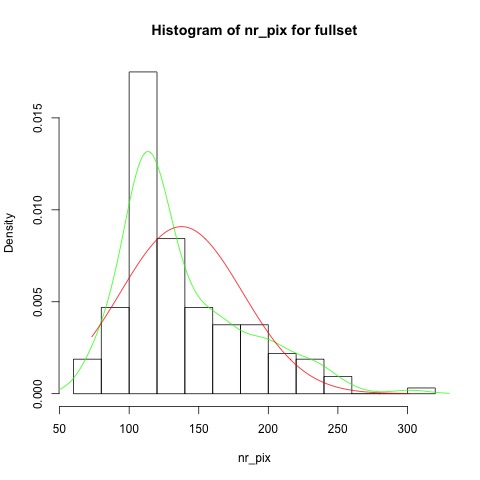


Figure Histogram of the distribution of nr\_pix for fullset

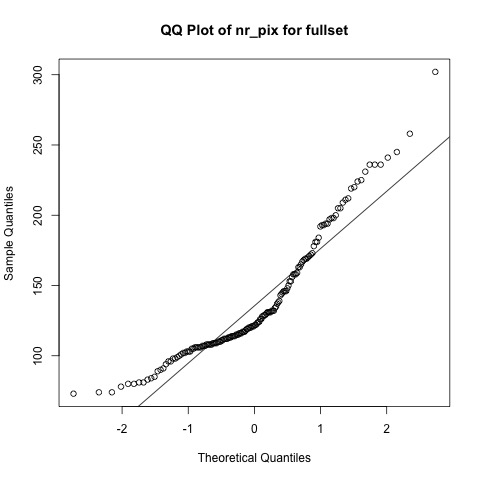


Figure QQ Plot of nr\_pix for fullset

For the shape of the distribution of feature *nr\_pix* for non-living things, Figure 11 shows that the modality is unimodal (ignoring the small peak at the left), and the skewness is symmetric. Figure 12 illustrates that the normality of the distribution is long tails.

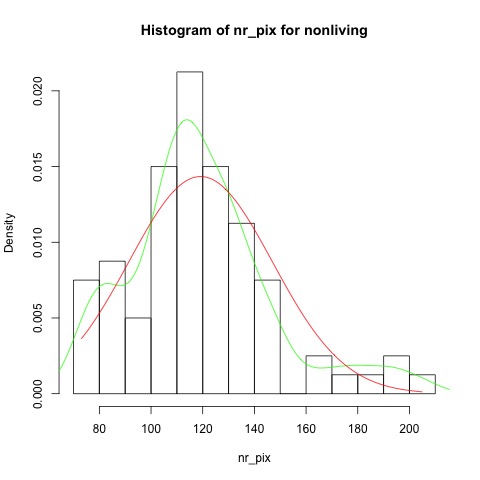


Figure Histogram of the distribution of nr\_pix for non-living

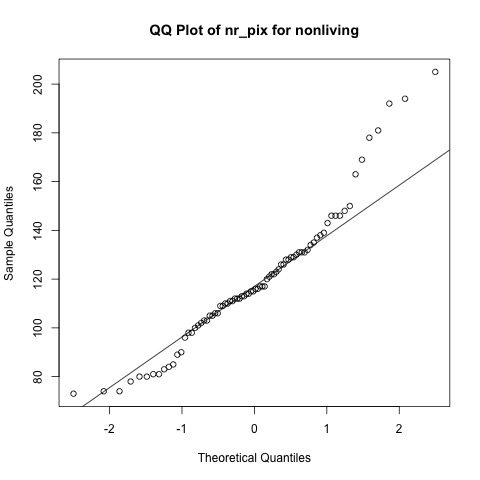


Figure QQ Plot of nr\_pix for nonliving

For the shape of the distribution of feature *nr\_pix* for living things, Figure 13 shows that the modality is unimodal, and the skewness is right skew. Figure 14 illustrates that the normality of the distribution is short tails.



Figure Histogram of the distribution of nr\_pix for living

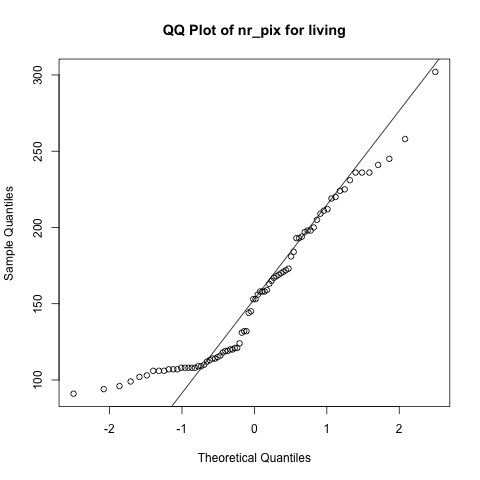


Figure QQ Plot of nr\_pix for living

#### height

For the shape of the distribution of feature *height* for fullset, Figure 15 shows that the modality is unimodal, and the skewness is left skew. However, it contains some outliers at the very left, which may be indicative of measurement error. Figure 16 illustrates that the normality of the distribution is left skew.

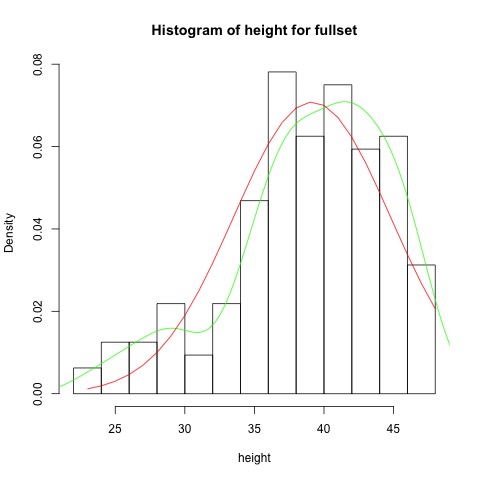


Figure Histogram of the distribution of height for fullset

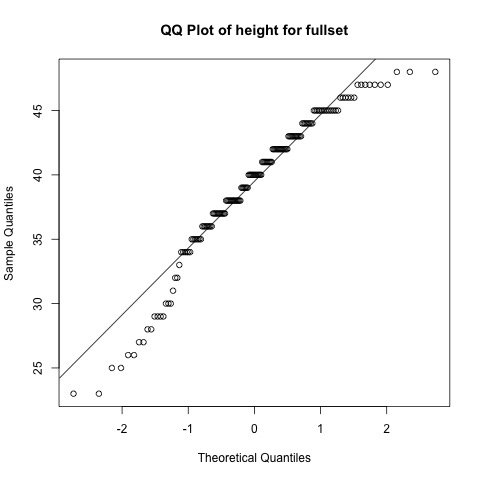


Figure QQ Plot of height for fullset

For the shape of the distribution of feature *height* for non-living things, Figure 17 shows that the modality is unimodal, and the skewness symmetric. Figure 18 illustrates the normality of the distribution is left skew.

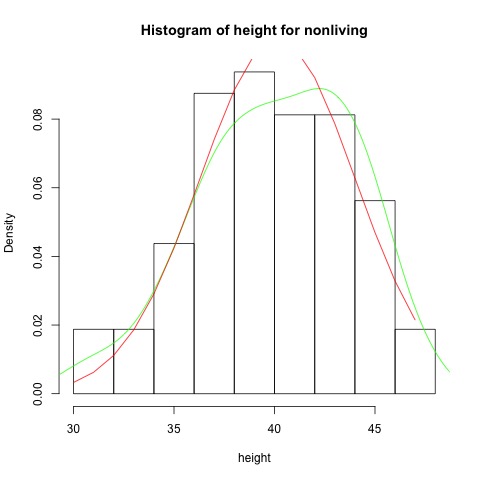


Figure Historgram of the distribution of height for non-living

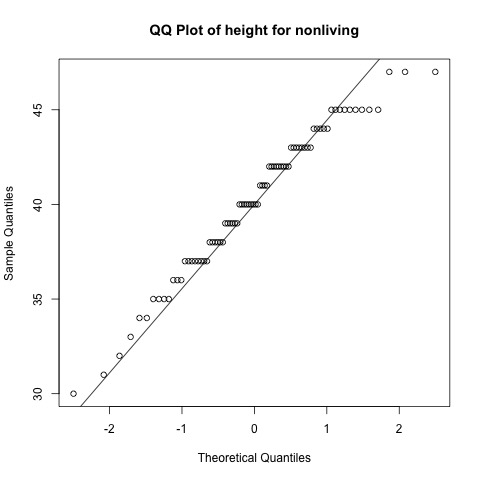


Figure QQ Plot of height for non-living

For the shape of the distribution of feature *height* for living things, Figure 19 shows that the modality is bimodal, and the skewness slightly left skew. Figure 20 illustrates the normality of the distribution is short tails.

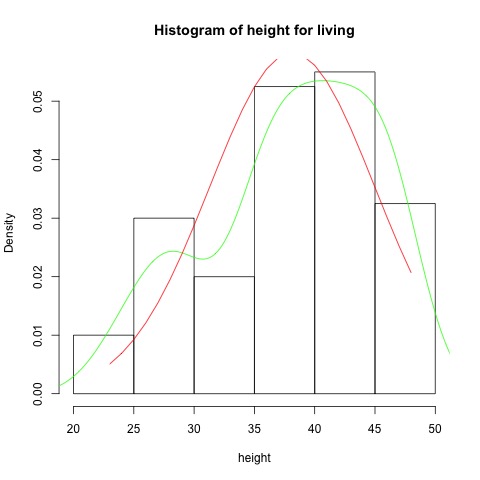


Figure Histogram of the distribution of height for living

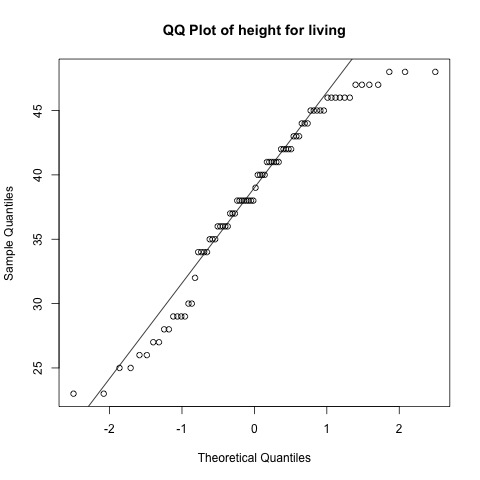


Figure QQ Plot of height for living

#### cols\_with\_5

For the shape of the distribution of feature *cols\_with\_5* for full set, Figure 21 shows that the modality is unimodal, and the skewness slightly right skew. It contains some outliers at the very right which may be indicative of measurement error. Figure 22 illustrates the normality of the distribution is right skew.

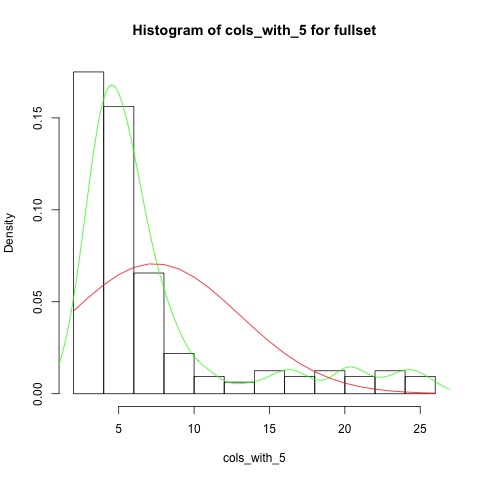


Figure Histogram of the distribution of cols\_with\_5 for fullset

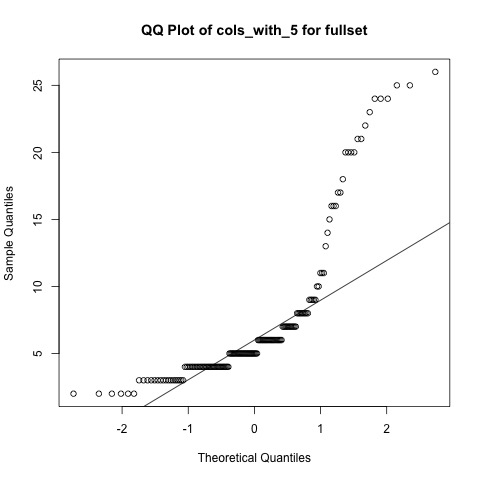


Figure QQ Plot of cols\_with\_5 for fullset

For the shape of the distribution of feature *cols\_with\_5* for non-living things, Figure 23 shows that the modality is unimodal, and the skewness is slightly right skew. However, it contains some outliers at the very right, which may be indicative of measurement error. Figure 24 illustrates the normality of the distribution is right skew.

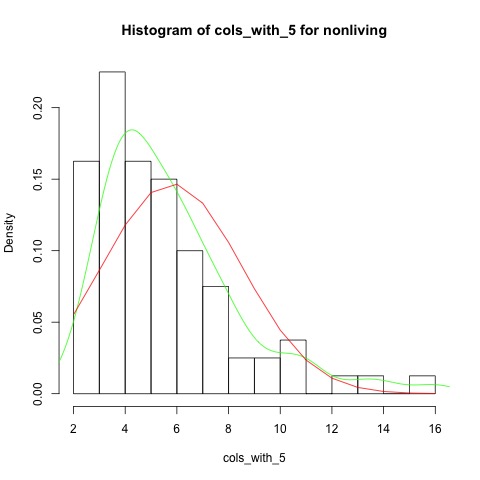


Figure Histogram of the distribution of cols\_with\_5 for non-living

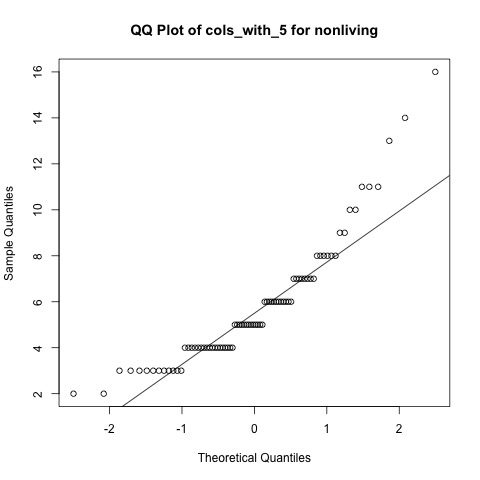


Figure QQ Plot of cols\_with\_5 for nonliving

For the shape of the distribution of feature *cols\_with\_5* for living things, Figure 25 shows that the modality is bimodal, and the skewness is slightly right skew. Figure 26 illustrates that the normality of the distribution is right skew.

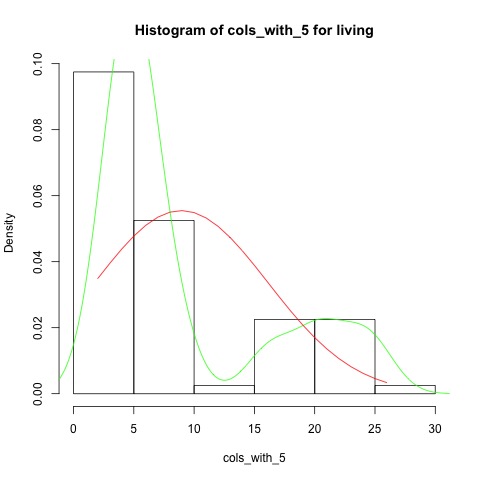


Figure Histogram of the distribution of cols\_with\_5 for living

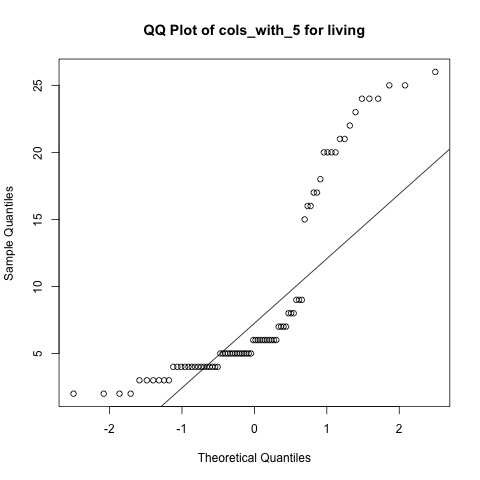


Figure QQ Plot of cols\_with\_5 for living

## Subtask 2

### Requirement

We need to generate summary statics for three groups of things/objects and perform analysis to discriminate things from different groups.

### STANDARD RANGE

Definition: the **STANDARD** **RANGE** of a feature is the range of , where mean and standard deviation are calculated from the values of the feature.

For example, if a feature has the mean of 10 and the standard deviation of 2, its STANDARD RANGE is .

### Reasoning

Assuming the values of each feature is normally distributed, we consider the means and standard deviations of the values from any two groups. Compared to any two groups, we calculate the **STANDARD** **RANGE** of every feature from group A, and compare that range with the range of the same feature from group B. If these two ranges do not overlap too much, it means it may be a valuable feature to differentiate the things between this two groups. The reason is that there are 65% values of the feature falling into the **STANDARD** **RANGE** (, and if the **STANDARD** **RANGE**s do not overlap, we have a good chance to put the things into the right groups by analysing their feature values.

For example, the mean and the standard deviation of values from group A are 5 and 5, respectively. It is believed that 65% of values in group A are in . The mean and the standard deviation of values from group B are 20 and 5 respectively which means that 65% of values in group B are in . When getting a value of 9 which is in , we are confident that the instance that the value of 9 is corresponding to is in group A.

### Implementation

We use the summary() function for each feature and generate the tables (Figure 27, Figure 28 and Figure 29) for three groups of things.

### Results

#### Variable types

* Numeric (discrete): *index, nr\_pix, height, width, rows\_with\_5, cols\_with\_5 ,neigh1, neigh5, left2tile, right2tile, top2tile, bottom2tile, concentration, crossness, nr\_regions, nr\_eyes, hollowness, straightness*
* Numeric (continuous): *span,verticalness,horizontalness*
* Categorical (string): *label*

#### Summary tables

These three tables were generated.

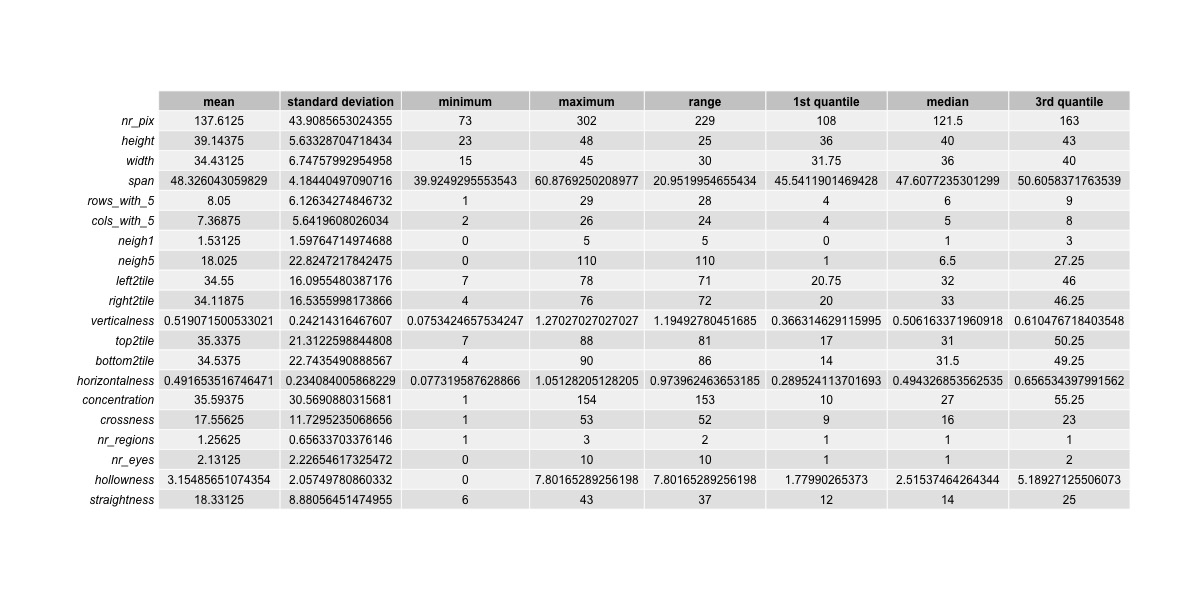


Figure Summary statics for fullset

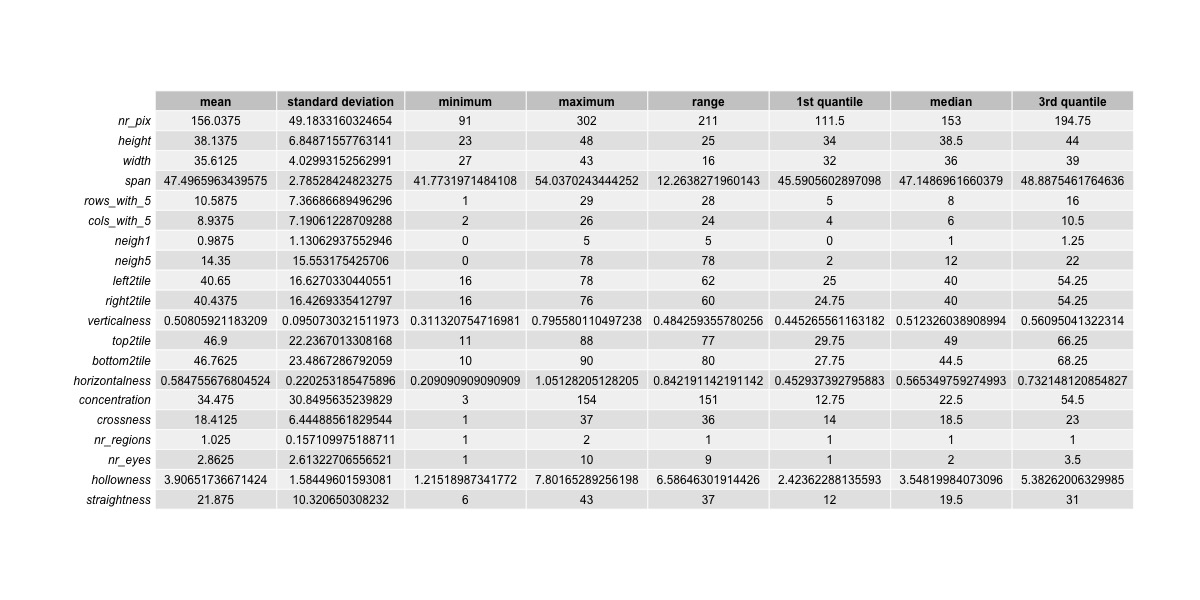


Figure Summary statics for living things

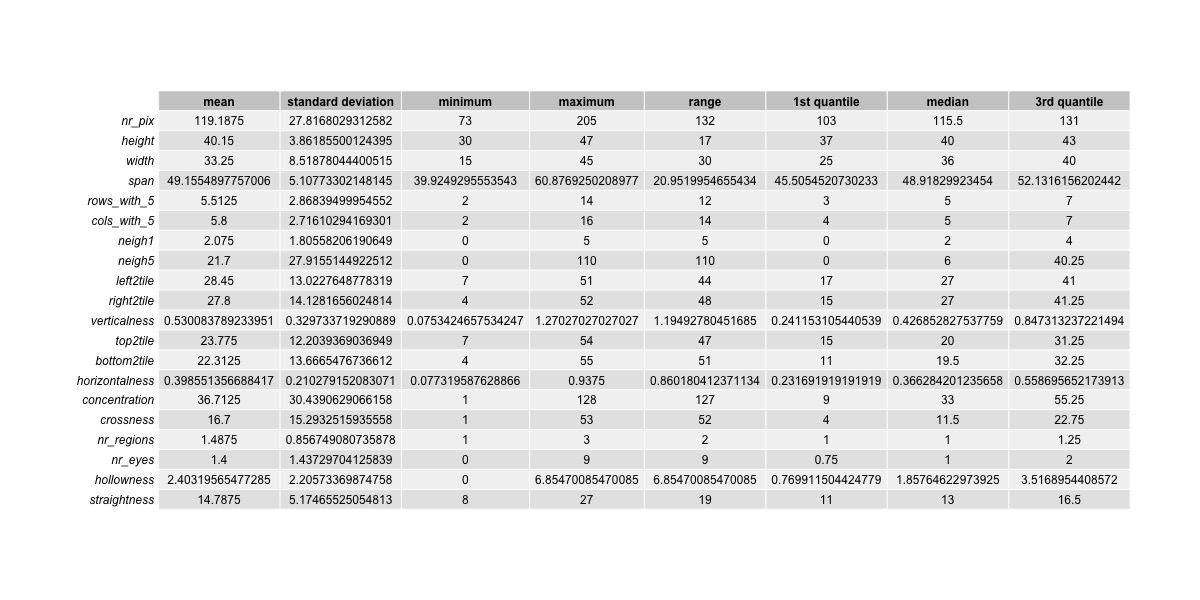


Figure Summary statics for nonliving things

#### Analysation

Unfortunately, after analysing, we did not find any two features that have **STANDARD** **RANGE**s not overlaying. However, we still got three features *top2tile*, *bottom2tile* and *horizontalness* that do not have too much overlaying and could be distinguishable between the groups living things and non-living things. We will examine each individual feature below.

#### top2tile

The feature *top2tile* has the mean of 46.9 and the standard deviation of 22.24 in the group of living things, which has the **STANDARD** **RANGE** of . Similarly, the mean is 23.78 and the standard deviation is 12.20 in non-living things where the **STANDARD** **RANGE** is .

Figure 30 shows the distributions of feature *top2tile* for living and non-living things in one histogram. It illustrates that the frequency for non-living things are higher than that for living things, when the value is below than 30. While the value is above 30, the frequency of living things is higher.

Thus, we can conclude that if an instance has the value of feature *top2tile* less than 30, the chance of being a non-living thing is higher. If the value is greater than 30, it is predicted to be a living thing. Because the separation of these two distributions are is considerable, we are confident in our conclusion.

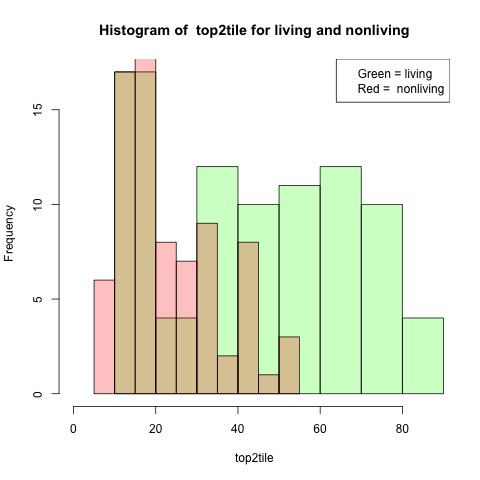


Figure Histogram of top2tile for living and nonliving

#### bottom2tile

The feature *bottom2tile* has the mean of 46.76 and the standard deviation of 23.49 in the group of living things, which has the **STANDARD** **RANGE** of . Similarly, the mean is 22.31 and the standard deviation is 13.67 in non-living things where the **STANDARD** **RANGE** is .

Figure 31 shows the distributions of feature *bottom2tile* for living and non-living things in one histogram. It illustrates that the frequency for non-living things are higher than that for living things, when the value is below than 35. While the value is above 35, the frequency of living things is higher.

Thus, we can conclude that if an instance has the value of feature *top2tile* less than 35, the chance of being a non-living thing is higher. If the value is greater than 35, it is predicted to be a living thing. Because the separation of these two distributions are is considerable, we are confident in our conclusion.

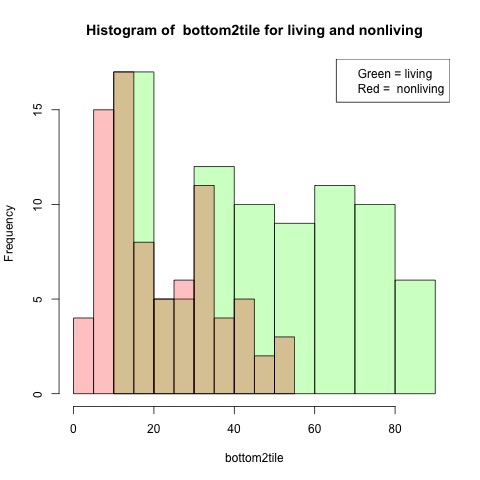


Figure Histogram of bottom2tile for living and nonliving

#### horizontalness

The feature *horizontalness* has the mean of 0.5848 and the standard deviation of 0.2203 in the group of living things, which has the **STANDARD** **RANGE** of . Similarly, the mean is 0.3986 and the standard deviation is 0.2103 in non-living things where the **STANDARD** **RANGE** is .

Figure 32 shows the distributions of feature *horizontalness* for living and non-living things in one histogram. It illustrates that the frequency for non-living things are higher than that for living things, when the value is below than 0.6. While the value is above 0.6, the frequency of living things is higher.

Thus, we can conclude that if an instance has the value of feature *top2tile* less than 0.6, the chance of being a non-living thing is higher. If the value is greater than 0.6, it is predicted to be a living thing. Because the separation of these two distributions is not complete, we only have moderate confidence in our conclusion.

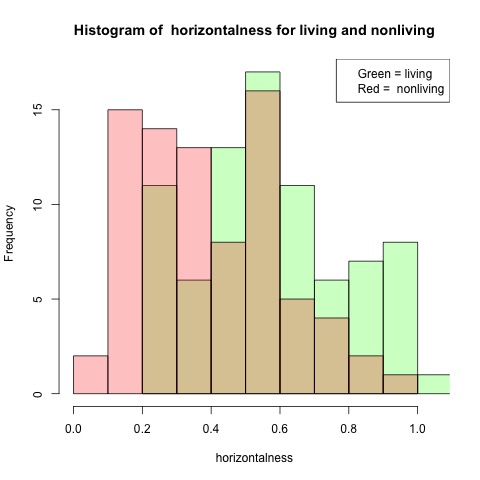


Figure Histogram of horizontalness for living and non-living

## Subtask 3

### Assumption

We assume the variable nr\_pix is randomly sampled from a population which is normally distributed (Devereux, 2019).

We assume thesevalues have been sampled without replacement, and of the population.

### Reasoning

The sample data meets these two requirements.

* Independence
* The population distribution is normal

We consider it is independence, because the values are randomly sampled without replacement and the sample size is greateer than 30, and less than of the population. Also, as the Assumption, the population is normal distributed.

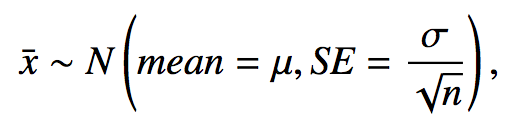
Thus, Central Limit Theorem (CLT) applies. We can get the estimated variance and the confidence interval for the actual mean of the population.

### Implementation

We calculate

* . The length of the data
* . The mean of the sample data
* . The standard deviation of the sample data

According to CLT, the distribution of the sample mean is

 (Devereux, 2019)

We then draw the distribution (Figure 30).

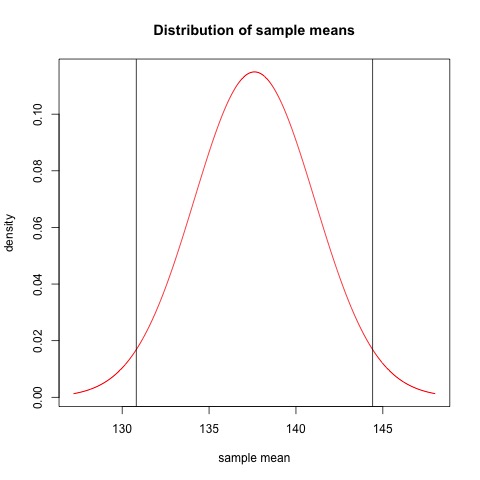


Figure Normal distribution of nr\_pix sample means

We assure the z-score is 1.96 for confidence.

We have the confidence interval

We have 95% confidence that the actual mean of the population is inside this interval.

The estimated mean of the population is . The estimated variance of the population is

With the mean() and sd() functions, the mean and standard deviation of the values of nr\_pix are calculated.

We then draw Figure 30 showing the normal distribution with the mean and standard deviation of the values of nr\_pix. To compare the theoretical normal distribution line with the actual distribution of nr\_pix, Figure 32 is the histogram of the distribution is drawn with the same xlim and ylim values.

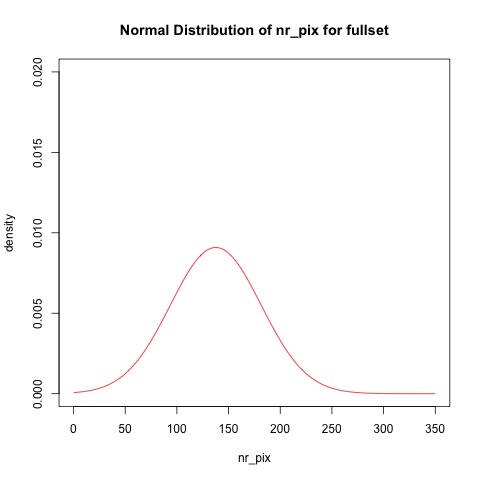


Figure Normal distribution of nr\_pix for fullset

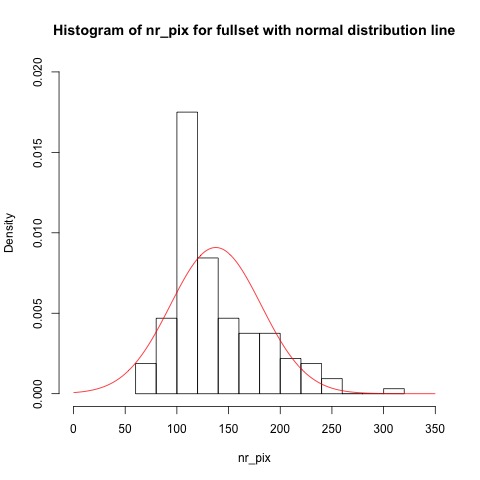


Figure Histogram of nr\_pix for fullset with normal distribution line

### Result

The estimated mean of the population is . We have 95% confidence that the actual mean of the population in between 130.809 and 144.416

The estimated variance of the population is

From the normal distribution with the estimated mean and variance, we do not consider the variable nr\_pix is normally distributed. It does not approximately match the normal distribution line, because of its prominent peak near to the value 100 and the almost-zero density for the values from 0 to 50.

## Subtask 4

### Assumption

We assume the variable nr\_pix is normally distributed. The mean and the standard deviation of the normal distribution are the mean and the standard deviation of the value from the full set dataset respectively.

### Implementation

With mean() and sd() functions, the mean and standard deviation of the values of nr\_pix are calculated. The qnorm() function is used to find out the quantile(cut-off) value that 95% of values are observations in the normal distribution is below the cut-off value. The cut-off value is what the question is asking because it is equivalent to the cut-off value that there is 5% (1 – 95%) probability that the sample value is above it.

We then draw Figure 33 showing the normal distribution with the mean and standard deviation of the values of nr\_pix and the vertical line where the cut-off value is.

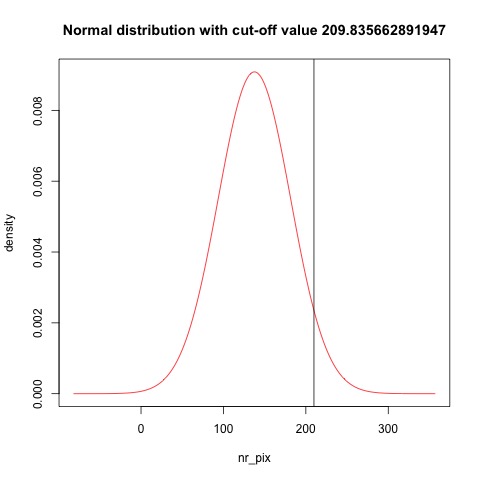


Figure Normal distribution of nr\_pix for fullset

### Reasoning

The reason we use qnorm() is that it returns the corresponding quantile given the percentile and the normal distribution.

### Result

From the qnor() function, we can get the cut-off value of 209.835662891947

## Subtask 5

### Implementation (part 1)

We will examine the skewness by both the statics and the histogram for each feature.

We generated a table (Figure 34) showing the skewness values for features 1 – 14 so that we can compare their absolute values. We consider the variable is (Lemos, 2018)

* Highly skewed, if the skewness value is greater than +1 or less than -1
* Moderately skewed, if the absolute skewness value is between 0.5 and 1
* Approximately symmetric, if the absolute skewness value is less than 0.5

And we will transform the highly skewed data.

Also, For each feature from 1 to 14, we generated a histogram of the distribution with a green line indicating the density of the distribution, and a red line showing the normal distribution of the sample mean and standard deviation, which also helps us to identify the extreme skewness.

### Results (Part 1)

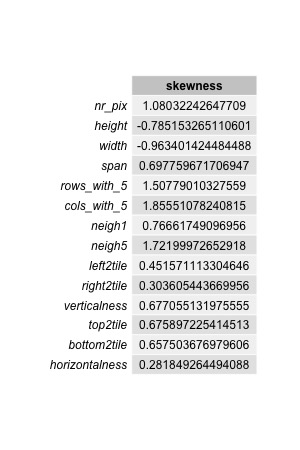
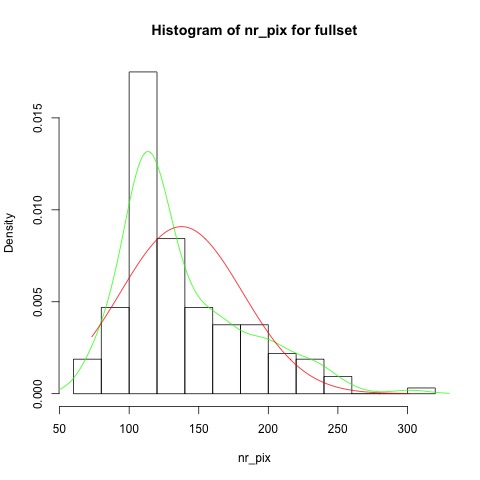


Figure Skewnesses of features 1 - 14

The statics show the feature *nr\_pix*, *rows\_with\_5*, *cols\_with\_5* and *neigh5* are highly skewed.

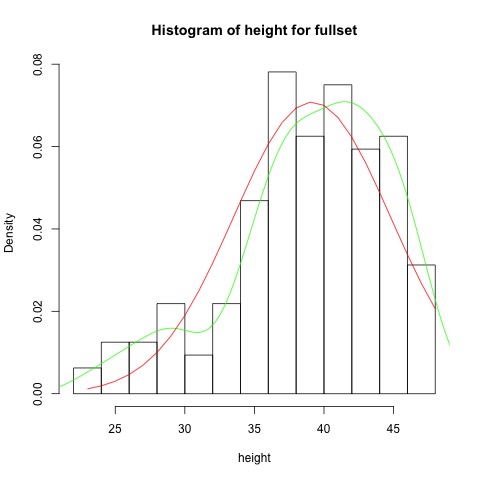
#### Feature 1

From the histogram, the distribution is considered to be extreme skew, and its skewness value is 1.08 Log transformation is required.



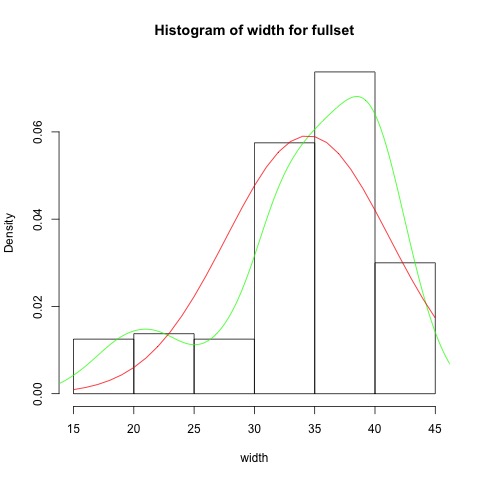
#### Feature 2

From the histogram, the distribution is not considered to be extreme skew. Transformation is not required.



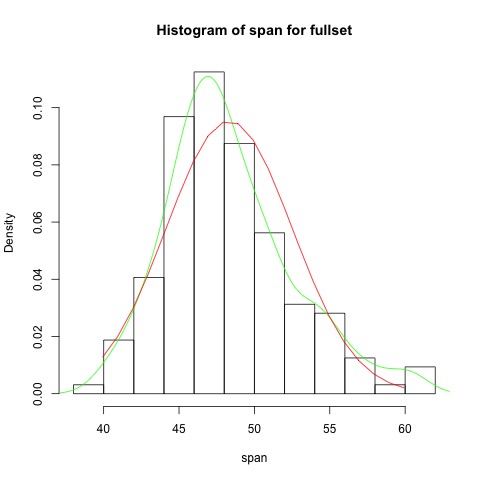
#### Feature 3

From the histogram, the distribution is not considered to be extreme skew. Transformation is not required.



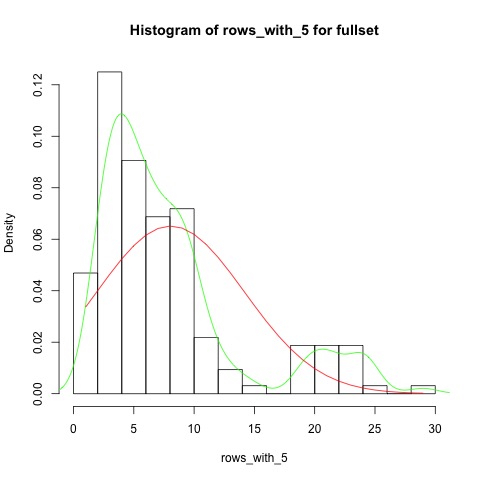
#### Feature 4

From the histogram, the distribution is not considered to be extreme skew. Transformation is not required.



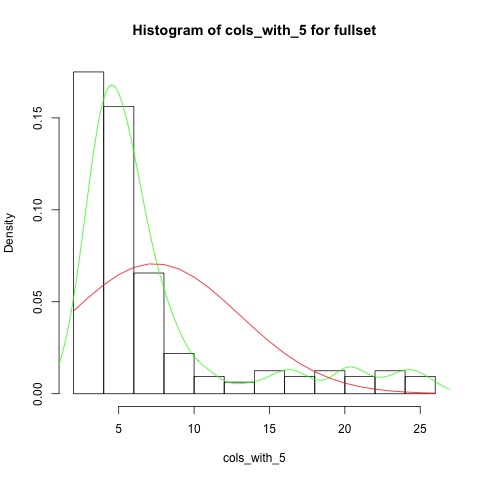
#### Feature 5

From the histogram, the distribution is considered to be extreme right skew, and its skewness value is 1.51. Log transformation is required.



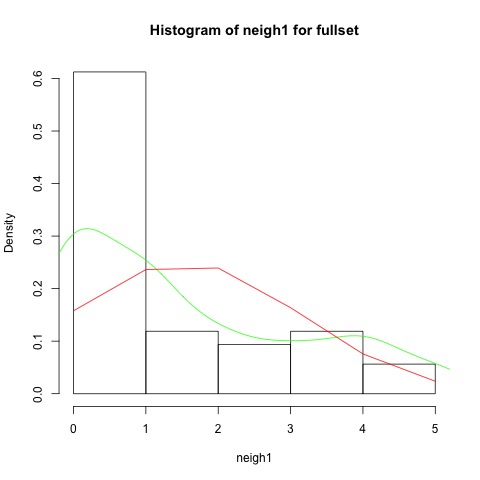
#### Feature 6

From the histogram, the distribution is extreme right skew, and its skewness value is . Log transformation is required.



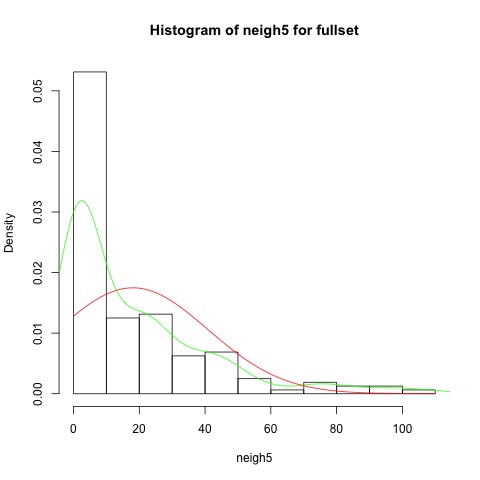
#### Feature 7

From the histogram, the distribution is right skew, but it is now extreme. Log transformation is not required.



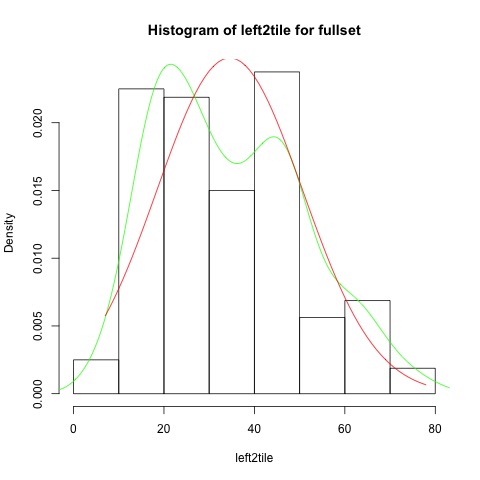
#### Feature 8

The histogram illustrates that the distribution is extreme right skew, and its skewness value is . Log transformation is required.



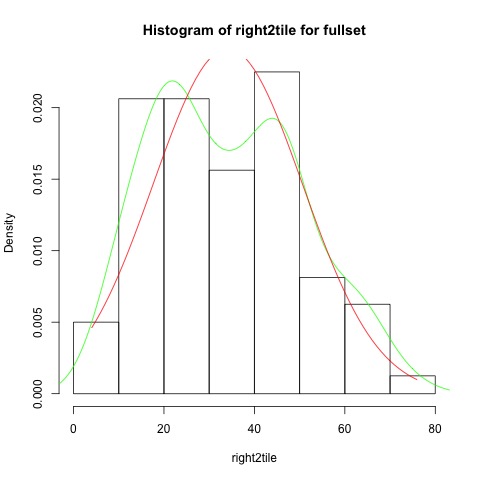
#### Feature 9

From the histogram, the distribution is not considered to be extreme skew. Transformation is not required.



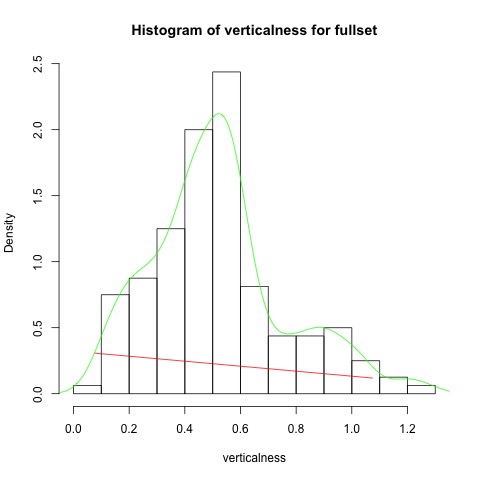
#### Feature 10

From the histogram, the distribution is not considered to be extreme skew. Transformation is not required.



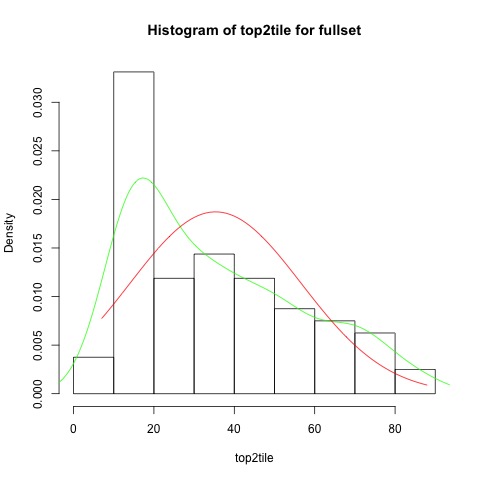
#### Feature 11

From the histogram, the distribution is not considered to be extreme skew. Transformation is not required.



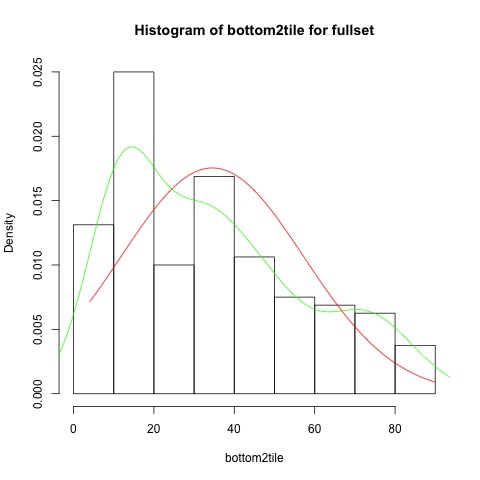
#### Feature 12

From the histogram, the distribution is not considered to be extreme skew. Transformation is not required.



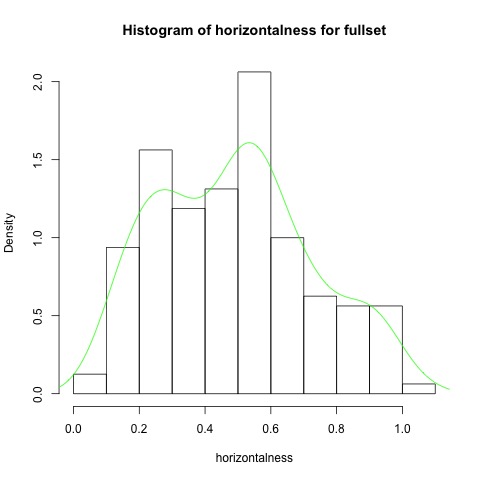
#### Feature 13

From the histogram, the distribution is not considered to be extreme skew. Transformation is not required.



#### Feature 14

From the histogram, the distribution is not considered to be extreme skew. Transformation is not required.



### Implementation (part 2)

For extreme skew data, logarithm function log1p() will be performed to the original data for the transformation. We then compute its new skewness value to make sure the skewness has been improved. We will redo the log1p() function until the absolute skewness value has been decreased to under 1. Finally, we redraw the histograms.

### Result (part 2)

From Results (Part 1), we concluded that we need to transform Feature 1, Feature 5, Feature 6 and Feature 8.

#### Feature 1

The distribution of the feature *nr\_pix* has extreme right skew. Log transformation will be performed.

The new distribution of the values of this feature is re-drawn (Figure 35).

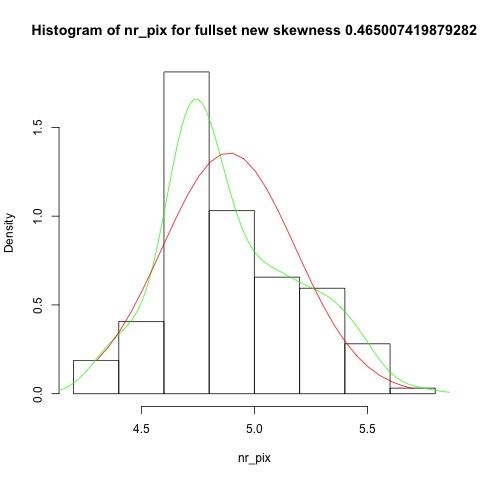


Figure Transformed data for feature nr\_pix

The new skewness value of the transformed data is 0.47, which is considered to be approximately symmetric.

#### Feature 5

The distribution of the feature *rows\_with\_5* has extreme right skew. Log transformation is will be performed.

The new distribution of the values of this feature is re-drawn (Figure 36).

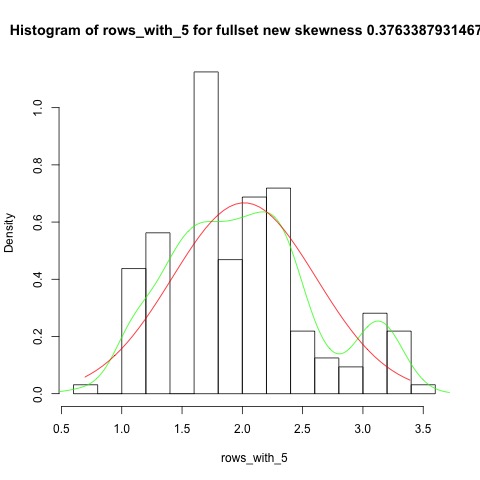


Figure Transformed data for feature rows\_with\_5

The new skewness value of the transformed data is 0.38, which is considered to approximately symmetric.

#### Feature 6

The distribution of the feature *cols\_with\_5* has extreme right skew. Log transformation will be performed.

The new distribution of the values of this feature is re-drawn (Figure 37).

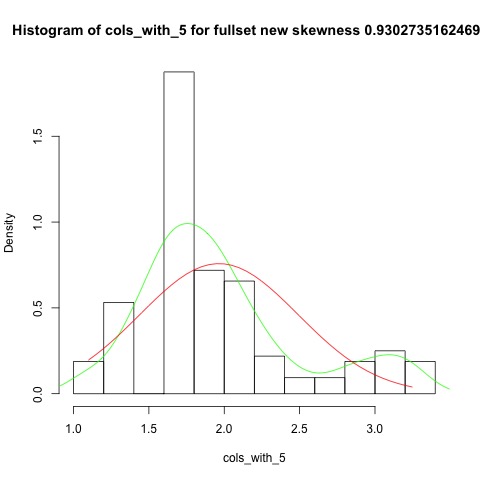


Figure Transformed data for feature cols\_with\_5

The new skewness value of the transformed data is 0.93, which is not considered to be extreme skew.

#### Feature 8

The distribution of the feature *neigh5* has extreme right skew. Log transformation is will be performed.

The new distribution of the values of this feature is re-drawn (Figure 38).

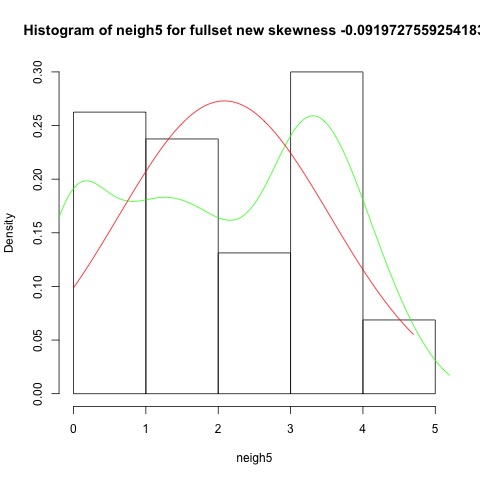


Figure Transformed data for feature neigh5

The new skewness value of the transformed data is -0.09, which is almost a perfect symmetric distribution.

## Subtask 6

### Assumption

As it states in the assignment 2 document (Devereux, 2019), we assume the significance level is 0.05 for hypothesis tests.

### Reasoning

We will be using Pearson correlation test to perform this task, because the distributions of feature *height* and *span* (Figure 42 and Figure 43) suggest that they are not extreme skewed and are close to normal distributions, which meet the requirement of Pearson correlation test.

A close up of a map

Description automatically generated

Figure Histogram of height for fullset

A close up of a map

Description automatically generated

Figure Histogram of span for fullset

### Implementation

With the data of features height and span, we can draw the following scatterplot (Figure 44) with a regression line (red) and a lowess line (blue). From the visualisation of the figure, it is believed that these two features span and height have positive linear association, but the association is weak.

A close up of a map

Description automatically generated

Figure Scatterplot for features height and span

We then perform a Pearson correlation test to verify the hypothesis. First, we have two hypothesis.

* Null hypothesis. The true correlation is equal to 0 (no linear association)
* Alternative hypothesis. The true correlation is not equal to 0 (linear association)

We will use R function cor.test() to perform the test. By analysing the p-value and the cor value, we can conclude the relationship between these two features.

### Results

The output of the Pearson correlation test is as Figure 45 where and

A screenshot of a social media post

Description automatically generated

Figure Correlation test result

As the p-value is less than the significant level value which is 0.05, we reject the null hypothesis and accept the alternative hypothesis. In other words, we believe the features span and height are linear associated.

We then check out the correlation coefficient value. According to the description of the correlation coefficient (Rumsey, 2019), the value suggests that features span and height have a weak uphill positive linear relationship.

## Subtask 7

### Requirement

Answer the question:

Is the nr\_pix feature useful to discriminate between the 4 different classes of wineglass, golfclub, pencil, and envelope?

### Reasoning

Since we need to test four dependent variables, using ANOVA is a good choice since it enables hypothesis tests on multiple objects. Also, ANOVA prevents type 1 error by modifying the significant level.

In the implementation section below, we will demonstrate that the variables nr\_pix of the objects wineglass, golf club, pencil and envelope meet the following requirements (To, 2019) to perform the ANOVA test.

* The population should be nearly normal
* The sample should be independent
* The population variances are equal
* Different groups should have the same size

### Implementation

#### Data visualisation

To visualise the data, we can draw figures showing the observations of the data in different perspectives.

Figure 46 shows the range of the observations. From visualisation, the means of the samples are different, and they are within-group variances are moderate.

A screenshot of a cell phone

Description automatically generated

Figure Observation of nr\_pix boxplot + dotplot

Figure 47 illustrate the densities of the data. From the figure, except the data of pencil, other objects have their own prominent peaks in different range and they barely overlap. However, the variance of the data of pencil is large, across the range of the other objects data.

A close up of a logo

Description automatically generated

Figure Observation of nr\_pix density

Figure 48 gives details of the observation. We can see there is a outlier in the data of envelope. The variance of the pencil data is large.

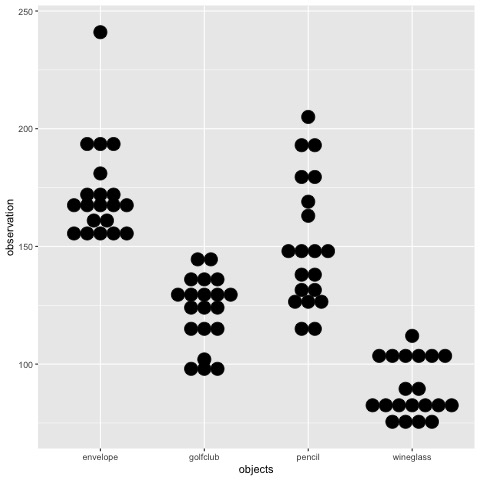


Figure Observation of nr\_pix dotplot

Figure 49 is a histogram of the data. We observe that the data of envelope, golfclub and wineglass have their prominent peaks and do not overlap too much.

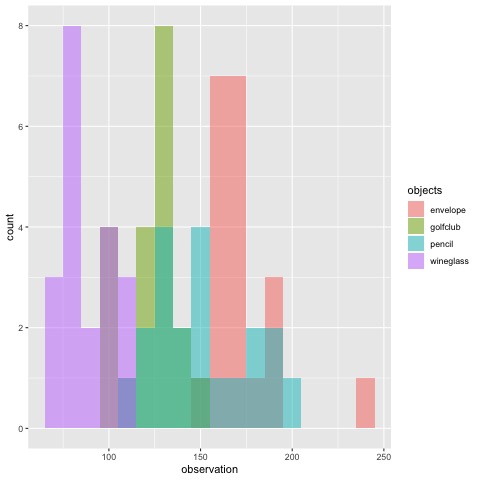


Figure Observation of nr\_pix histogram

According to the data above, we can see some obvious difference between objects, we think there is at least one mean from one group is different, but we now need to perform ANOVA test to prove it.

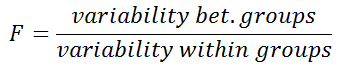
#### ANOVA test

First, as the section Reasoning says, the data meet the requirements for perform the ANOVA test.

Secondly, we have two hypothesis.

* Null hypothesis. The actual means of the population are the same across these four objects.
* Alternative hypothesis. At least one mean from one group is different than other groups

The variable F is

 (Devereux, 2019)

To calculate the F value, we feed the data into the R script function aov(), and apply the summary() function to it. We get the output as Figure 50 which is a table of values. We will give explanation (Devereux, 2019) for each value in the table.

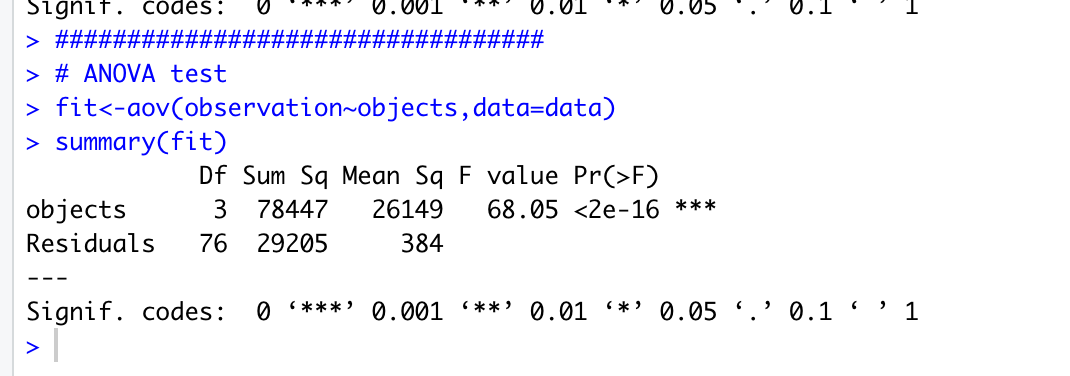


Figure Output of the ANOVA test

##### Degree of freedom

The first column Df is short for Degree of freedom.

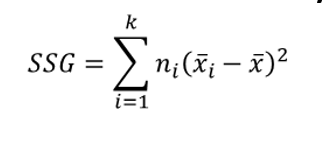
The first value 3 is , where k is the number of groups (i.e. objects). There are 4 groups in our data, so the value is .

The second value 76 is the Df for error *dfE* = *dfT* - *dfG where dfT = n – 1 where n is the total sample size.* There are 80 non-living instances, so *dfT = 80-1=79.* Then, *dfE* = *dfT* - *dfG = 79 – 3 = 76*

##### Sum of Squares

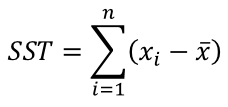
The second column Sum Sq is short for Sum of Squares

The first value is SSG = 78447

 (Devereux, 2019)

*“Where  is the size of each group, is the average for each group, and* 𝒙 ̅is *the overall mean”* (Devereux, 2019)

The second value is SSE = 29205.

 (Devereux, 2019)

where 𝒙 ̅is the overall mean.

Thus, the value SSE = SST – SSG

##### Mean Square

The third column Mean Sq is short for Mean Square.

The first value is

The second value is

##### F value

The forth column is F value.

##### P value

The fifth column is P value

### Result

Because the p value is less than 0.05 which has been assumed to be the significant level, the null hypothesis is rejected and the alternative hypothesis is accepted. We believe that for the feature *nr\_pix*, At least one mean from one group is different than other groups.

Hence, we can conclude that the *nr\_pix* feature is useful to discriminate between the 4 different classes of wineglass, golf club, pencil and envelope.

## Subtask 8

### Reasoning

We will perform a large number of randomisation tests on these four groups of non-living things. However, the traditional randomisation test compares the association of only two groups of variables, but there are four groups of variables.

The solution is that instead of comparing the difference of means between two groups, we apply ANOVA test to these four groups and compare the F-values of these groups. Thus, we have the following two hypotheses.

* Null hypothesis. The actual means of the population are the same across these four objects.
* Alternative hypothesis. At least one mean from one group is different than other groups

### Implementation

We first apply ANOVA test to the original data of four groups, we got the original F-value.

Then we will perform a series of randomisation tests. The total number of tests is set to be 10000. For each test, we shuffle the whole data, and randomly sample twenty elements for each group (four groups in total). We perform the ANOVA test to these four randomly sample groups and generate the F-value. If the F-value is greater than the original F-value, we count this randomisation test as a successful test.

After 10000 randomisation tests, the number of successful tests is calculated, which is the P-value. Figure 51 is the result of one of our examples.

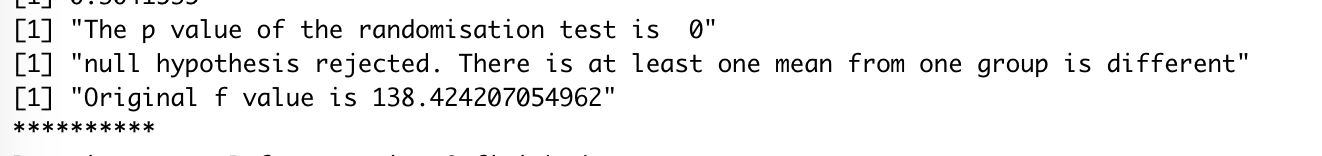


Figure Subtask 8 result

which is less than the significant level. We reject the null hypothesis test and accept the alternative test.

### Result

We can conclude that for the feature hollowness, At least one mean from one group is different than other groups. Hence, the feature hollowness is useful to discriminate between the 4 different classes of wineglass, golf club, pencil and envelope.

## Subtask 9

## Subtask 10

### Reasoning

We use pairwise t test on the 4 groups of non-living things because pairwise t test helps easily figure out all the P-values for each combination. Also, it has an adjustment function that reduces the chance of getting into type 1 error.

### Implementation

Like what we did in Subtask 7, we extract the data of the feature 2 – 6 for all non-living things. For each feature, we perform ANOVA test to each feature (Figure 52). It gives a maximum F-value of 205.16721 for feature *width*.

A screenshot of a cell phone

Description automatically generated

Figure Output of ANOVA tests on features

We then apply the pairwise t test function to the data of feature *width*, with the adjustment function of Bonferroni. To prevent type 1 error, Bonferroni is used to adjust the P-values to reduce the chance that we incorrectly rejected null hypothesis.

The pairwise gives the output of Figure 53. The figure illustrate the P-value for the each combination of group pairs.

We notice that these P-values are less than the significant level

* P-value(wineglass~envelope)
* P-value(wineglass~golfclub)
* P-value(wineglass~pencil)

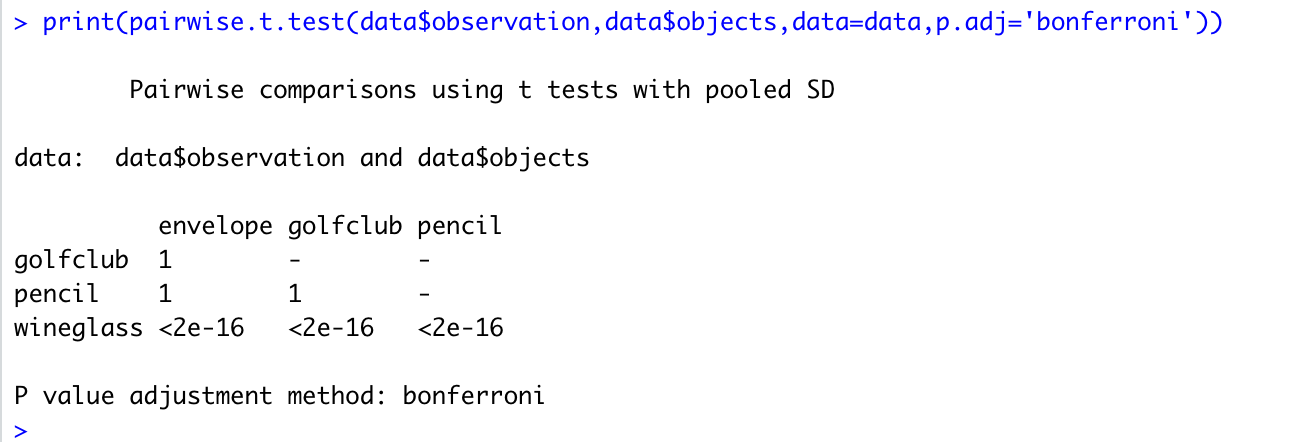


Figure Output of pairwise t test

## Result

# Conclusions

# References

Devereux, B., 2019. *Assignment 2 – CSC3060 “AIDA”.* [Online]   
Available at: https://canvas.qub.ac.uk/courses/8433/files/452305/download?wrap=1  
[Accessed 12 November 2019].

Lemos, M., 2018. *A hands-on tutorial about Log Transformations using R language.* [Online]   
Available at: http://rpubs.com/marvinlemos/log-transformation  
[Accessed 15 11 2019].